

Research Article

Tunneling Beneath the ${}^4\text{He}^*$ Fragmentation Energy

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Abstract

The repulsive Coulomb barrier between deuterium nuclei is reduced in length and height by a catalytic mechanism involving optical phonons and electric fields in a lattice. If this mechanism induces the formation of $\text{D}^- \text{D}^+$ pairs, the tightly bound and energetic electron pair (a “lochon” in the D^- ion) becomes an attractive force between the nuclei. The lattice constraints and slow collision processes force the ions into a near 1-D configuration within the lattice that deepens the electron ground-state potential well. This permits the electron pair to remain closely bound to one deuteron and to do work in bringing the $\text{D}^- \text{D}^+$ pair together. The work done reduces the nuclear-mass deficit (transferring it to electron kinetic and field energy) and that, along with the reduced Coulomb repulsion of the nuclear protons, brings down the helium nuclear-energy levels of the fusing pair and raises the ${}^4\text{He}$ fragmentation level. The proposed model accounts for the observations in condensed-matter nuclear science (CMNS) of excess heat (in both p–p and d–d reactions) and the differing observations (or for the absence) of tritium, ${}^3\text{He}$, neutrons, and ${}^4\text{He}$. The variation (unpredictability) of results (inherent in the many experiments) and evidence for transmutation, heretofore stumbling blocks to acceptability of CMNS, is now perhaps a validation of its existence. All major observed CMNS processes are addressed by the model.

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PACS: 21.10.Dr Binding energies and masses, 25.10.+s Nuclear reactions involving few nucleon systems, 25.30.-c Lepton-induced reactions, 25.60.Pj Fusion reactions, 25.90.+k Other topics in nuclear reactions: specific reactions, 27.10.+h $A \leq 5$

1. Introduction

The Fleischman–Pons effect, observed in a palladium lattice electrolytically loaded with deuterium, is a release of energy greatly in excess of that possible by chemical means. The explanation proposed for the effect (a low-kinetic-energy nuclear-fusion of two-deuterium atoms) and the experimental results violated three known aspects of deuteron (d–d) fusion in Nuclear Physics. These are:

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1. *Ultra-low probability of reaction:* Tunneling of deuterons must occur through a much longer and higher inter-nuclear Coulomb barrier than could be penetrated at the rates required to provide the excess heat observed.
2. *Fragmentation and fragmentation ratio:* The high fragmentation rates that would result from conventional penetration of the d–d Coulomb barrier and the formation of an excited ${}^4\text{He}$ nucleus (${}^4\text{He}^*$) are not observed. The fragmentation *ratio*, n:p, from $\text{D}+\text{D} \Rightarrow {}^3\text{He}+\text{n}$ and $\text{D}+\text{D} \Rightarrow \text{T} + \text{p}$ is expected to be $\sim 50:50$ (neutron + ${}^3\text{He}$ and proton + ${}^3\text{H}$ emission are considered to be nuclear “ash”).
3. *Decay paths from excited states of ${}^4\text{He}$:* No energetic gamma rays from direct de-excitation of fused D–D nuclei to the ${}^4\text{He}$ ground state (or products from another mechanism for delivering nuclear energy to the lattice) are observed.

Furthermore, subsequent low-energy-nuclear-reaction (LENR) research has often failed to reproduce the effect, has produced a large variety of (instead of consistent) results, and has provided strong evidence of changes in elemental composition (transmutation [1]) that is not possible from simple fusion reactions. Various models have been proposed to support the multiple experimental results and to overcome the arguments against a nuclear process. Few have been able to answer all of these challenges. None has yet been accepted, even by a large number of LENR researchers.

The present authors have developed a model ([2–5] reviewed briefly below) to solve the first of these problems using accepted physics of the solid state for the greater stability (perhaps cyclic) of charged sites relative to uncharged sites in some crystal lattices [6]. This knowledge was applied to the PdD lattice to suggest paired electrons in the same state (i.e., s-orbit in a D^- ion) becoming a local-charged Boson – the “lochon” – and the resulting $\text{D}^- \text{D}^+$ ion pairs being attractive rather than being repelled by the normal d–d Coulomb barrier [7]. The present work shows how extension of this lochon model supports the reduction in total energy of the colliding nucleons, and thereby explains most of the other experimental results observed in the field (including items 2 and 3 above).

The next sections describe the Lochon model, its extension, and its implications - from the PdD lattice sites, to the d–d near-field, and to the nuclear-interaction region. The nuclear issues are then addressed along with the mechanisms whereby the extended model is able to explain even the unexpected observations of LENR. Two appendices provide details of the extended-lochon process and address some applicable semi-classical physical-property issues of electrons and orbits that are never mentioned in quantum-mechanics texts and papers. A final appendix mentions a mathematical construction for a deep, bosonic, atomic orbital that might be verified by the experimental LENR results and the extended-lochon model.

2. Lochon Model

We have previously presented a model whereby the repulsive Coulomb barrier between hydrogen (deuterium) nuclei is reduced in height and length, perhaps by orders of magnitude [2]. This lochon-catalyzed-fusion mechanism, involving longitudinal optical phonons and local electric fields (internally or externally generated) in a crystal lattice that induce the formation of $\text{D}^- \text{D}^+$ pairs, increases the low-energy-tunneling probability by more than 100 orders of magnitude relative to that predicted from models based on multi-MeV deuteron-beam experiments [2].

We are dealing with a composite system (PdD_x) where two types of atoms or ions exist. Thus the primary lattice is palladium and the sub-lattice is hydrogen (deuterium). However, for our situation, the most relevant modes may be the interface phonon modes. The solutions to the quantum mechanical equations representing this system correspond to localized optical-phonon modes near the interface. The optical phonon mode of interest has the deuterons, beating against each other at the sub-lattice phonon frequency ($\sim 10^{14}/\text{s}$). The reduced dimensionality at an interface, or at a linear defect, deepens the potential well, thus creating higher-frequency phonon modes. These higher-energy modes create resonant electrostatic fields that are strongly coupled with the electrons confined in the layer. The addition of laser stimulation [2] increases the resonant phonon-field amplitudes, the $\text{D}^- \text{D}^+$ pair production, and the energy at which the local Coulomb barrier is encountered. This external resonant field can be adjusted to selectively stimulate the

higher-frequency modes and the counter moving deuteron modes. Phonon-induced electron pairing in a deepened well provides a basis for filling the deuterium's electron ground-state s-orbital that further localizes the pair [8] and binds it to a deuteron during its resonant oscillations within a lattice site.

The proposed electron pair would result in sub-lattice $D^- D^+$ pairs [9] and become more than strong screening; it would become an attractive force between the nuclei [5]. Thus, as the deuterons approach each other closely and deeply penetrate the D^- distributed-electron Coulomb field, the residual proton-proton (or d-d) Coulomb barrier is found to be much reduced, in height as well as in length. With the resulting enhanced barrier-penetration probability, the energy level of nuclei with reasonable tunneling probability may drop from the multi-100 keV range down into the many eV range, thus leading to low-energy nuclear reactions.

In this early version of our model (which was only concerned with the barrier penetration problem), normal tunneling of deuterons is into resonant excited $^4\text{He}^*$ nuclear states at energy levels above the fragmentation levels [10]. Thus, even if the Coulomb barrier is overcome by the tightly-bound electron pair and fusion is possible, the major observations of LENR (e.g. more heat than accounted for by neutron producing reactions) are not possible. This requirement of tunneling into states above fragmentation is dictated by the mass deficit ($Q = 23.8$ MeV [11]) between the two colliding D atoms and the resultant ^4He atom. Therefore, even with no incident kinetic energy, a deuteron pair has too much mass energy to tunnel beneath the fragmentation levels [12] at 20.6 and 19.8 MeV above the ^4He ground state. Nevertheless, the model was successful in providing a mechanism (with mathematical predictions of fusion rates consistent with observation) to counter arguments against LENR (item 1 above).

3. Extended Lochon Model

In a more detailed study of the lochon model, new and unexpected effects are found. Just as slow-motion photography can reveal unsuspected processes, the study of low-energy collisions between charged particles (i.e., eV compared to MeV) has provided some surprises. It is the non-equilibrium conditions of a “slow” $D^- D^+$ collision in a linear sub-lattice or lattice defect that provides a possible answer to the nuclear ash problem of CMNS (item 2 above). The deuteron motion is slow relative to the bound-electron motion. This distinction allows us to separate their actions and use the Born–Oppenheimer approximation to solve for the electron quasi-steady-state parameters, step-by-step, as the $D^- D^+$ pair approach each other over the lattice barrier separating them (and afterwards, Appendix A).

The D–D molecular potential well deepens as an extended D_2 molecule is being confined to two dimensions (Fig. 1) [13] by the lattice and Coulomb fields. During this process, the electron potential well also deepens (by reduced dimensionality and by the quadratic Stark effect from the confining lattice electric fields). A deepening of the electron potential wells does not necessarily mean that the electrons go deeper into the well; they must lose total energy to do that (although they gain kinetic energy in the process). However, being in a ground state ($l = 0$, with no lower energy states having angular momentum) they cannot directly radiate photons or generate phonons. (This would be a highly forbidden transition, since both processes require a change in angular momentum of $\Delta l = 1$). Because of the differences in resonant frequencies involved, indirect radiation of energy (via near-field coupling with lattice phonons) is slow. Nevertheless, in a critical concept provided by Tom Barnard [14], a mechanism is provided whereby these electrons may dissipate energy as the separation of the D– D^+ pair is reduced.

Since work is done by the electrons during this movement (they transfer energy to the deuterons), they fall further into the deuterons deepening Coulomb potential well. Part of this work is a result of “lochon drag,” which is analogous to phonon drag effects [15] on electrons in a lattice. Being deeper in the well means that one or both of the paired electrons is less likely to transfer to the potential well of the other deuteron during the process. This is a *critical assumption of the model* [16].

Since this electron pairing is a possible state, quantum mechanics can calculate its energy relative to that of zero or single-electron occupancy [6]. However, the probability of being in that state depends on the energy of the electron

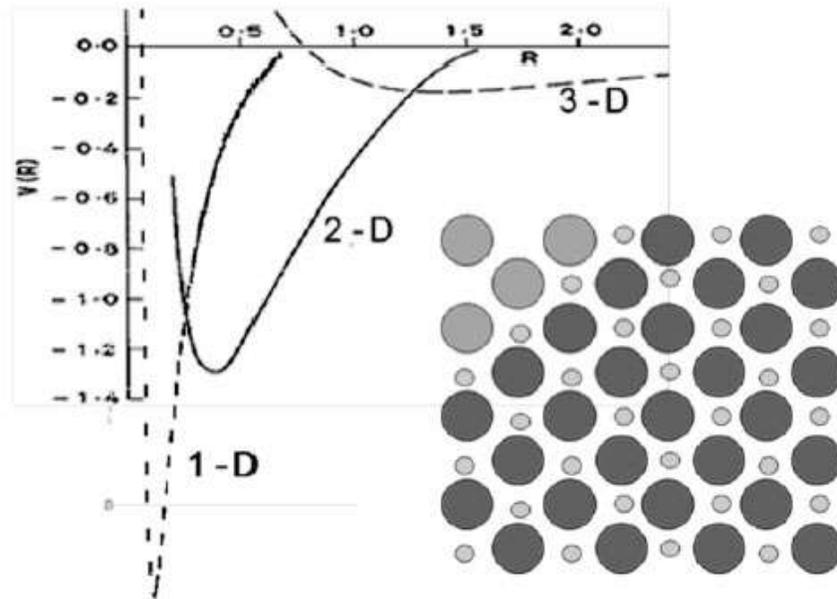


Figure 1. Molecular potential well for 3-D, 2-D, and 1-Dimension hydrogen-molecule configurations using atomic units ($R = 0.53 \text{ \AA}$ and $V(R) = 27.2 \text{ eV}$). The PdH lattice represented here (in planar view) includes an interface at which the tri-linear H sub-lattice is reduced in dimensionality.

pair and the local Fermi levels and electric fields; and these in turn depend on the recent history of the $D^- D^+$ pair. This is thus a time-dependent calculation. A consequence of the electron pairing in this model is that a portion of the electric-field energy of the $D^- D^+$ pair can be converted into work to overcome the lattice barrier (many-eV range) and the d-d Coulomb barrier (keV to MeV range) as they get closer. The effect of unpaired electrons, relative to that of paired electron(s), for LENR has been explored and found to be of little consequence.

3.1. Slow interactions

Nuclear physics collision experiments are diabatic. The equilibrium electron-energy levels do not have time to change before the event is over. On the other hand, the critical portion of the $D^- D^+$ interaction in a lattice is adiabatic. The “slow” motion of the converging deuterons allows hundreds of electron orbital cycles to occur during each step and therefore allows the electrons time to experience and respond to the changing fields. Furthermore, nuclear physics experiments are unlikely to see any of this $D^- D^+$ pairing effect unless the target deuterons have a reasonable probability of being in the negative ion state at the moment of collision. On the other hand, under the influence of lattice optical-phonon motion, that moment may be precisely when this state is most likely. A deuteron-beam experiment would have only a low statistical probability of involving a negative deuterium ion. Also, the mathematical interpretation of nuclear physics experiments under its low-energy (e.g. $\sim 5 \text{ keV}$) collision conditions would only indicate a higher Coulomb screening [17]. This interpretation *may be* appropriate for a deuteron with bound electrons. However, there are aspects of the LENR experimental results and of this model that any nuclear physics experiment is unlikely to see.

As the bound electrons move deeper into the D^- Coulomb potential well, the cancellation of external electric fields (of the electron and proton) reduces the external field energy (potential energy) and therefore the “size” and (initially

very slightly) the mass of the charged particles [18]. Since energy is conserved, part of this loss in field energy goes into the increased kinetic energy of the electrons (T_e), part into the increased kinetic energy of the deuterons (T_d), and part into increasing the inter electron–deuteron electric fields as the oppositely charged particles move closer together (Appendix A). However, just as the electrons do work in bringing the deuterons together, the deuteron and electron pairs must have work done on them to move them closer together. Thus, there are compensating field contributions from the e–e and d–d interactions as well. The net result of this 3 or 4-body interaction is that the tightly-bound, energetic, electrons (lochon or $e^\#$ s) and deuterons lose total energy (they have more KE, but have moved even deeper into the local Coulomb wells). With proximity, the D^-D^+ attractive Coulomb potential grows, and collapse of the D^-D^+ pair is accelerated. Nevertheless, the initial energy expended in overcoming the lattice barrier keeps the D^-D^+ pair in the adiabatic regime (at low velocity) until the pair gets very close (~ 10 pm?). As the pair gets still closer together, the D^-D^+ Coulomb potential dominates the lattice barrier and the closing velocity increases. However, during this same period, the electron kinetic energy also increases greatly so that the relative velocities (electron to deuteron) are maintained in the adiabatic regime.

The electron's kinetic-energy-increase and their movement deeper into the Coulomb well about the deuteron causes them and their orbit to “shrink” (Appendices B and A). The electron deBroglie wavelength decreases with increased velocity and, as it spirals in, its external-field energy is further “cancelled” by that of the proton. With an increase in energy from the $T_e = \text{multi-eV}$ range of electrons in sub-lattice deuterium atoms to the keV range of a bound electron as it approaches the deuteron, the deBroglie wavelength is reduced by an order of magnitude. As the $e^\#$ kinetic energy increases to the 100 keV range, the wavelength drops by $10\times$ again and approaches that of the electron Compton radius. However, by this time, the peak electron field (and therefore the electron center of “mass”) has shifted to within 100s of Fermi of the nucleus.

3.2. Electron–proton interaction in the 1–10 fm range

As the electron moves even closer to the nucleus (within 10 fm), its instantaneous kinetic energy continues to increase; but, it begins to lose its identity and may no longer be considered a separate entity (Fig. 2). The $e^\#-p$ pair has become a relativistic rotating dipole field (monopole + quadrupole field, if two bound electrons are present). The cancelled charge far-field energy has been replaced by near-field, electromagnetic and relativistic-mass energy. In support of this proposed semi-classical kinematic model for the (brief?) existence of tightly bound electron pairs, recent mathematical work [19] uses a solution of the Klein–Gordon equation to indicate the possibility of a deep energy level [20] in the hydrogen atom (Appendix C) for a charged boson, such as the lochon.

Figure 2a shows the consequences of electron–proton proximity on the electric potential (assuming stationary charges) as an example of the size/shape change effect mentioned above and in Appendix B. (Resolution of Fig. 2b is insufficient to show details at the sub-fm scale.) In the 60 fm range and assuming the classical-electron radius ($r_e = 2.82$ fm), the electron and proton potentials are clearly delineated. At 10 fm, the potentials significantly alter each other and the “effective” charge is less than 1 for either of the particles (the dipole approximation still works). As the ($e^\#p$) pair shrinks further, the electric field of the electron is progressively cancelled by that of the proton and the residual proton-charge radius is limited to femtometers. The fact that there is any residual charge is attributable to the extra mass and relativistic nature of the proton's inner structure.

What do these changes mean to the problem at hand? To first order, we'll assume that the *changes* in electron size, fields, and deBroglie and Compton radii can be ignored. The electron will be considered as a classical charge. We will treat the proximate electron–proton as a small dipole rather than the large structure that would result from using the deBroglie or Compton radii. The Heisenberg Uncertainty Principle, as applied to the tightly bound electrons(s), will be modified by the proximate presence of the proton(s) so that the kinetic energies required to shrink free electrons to nuclear sizes are no longer in the 100 MeV range.

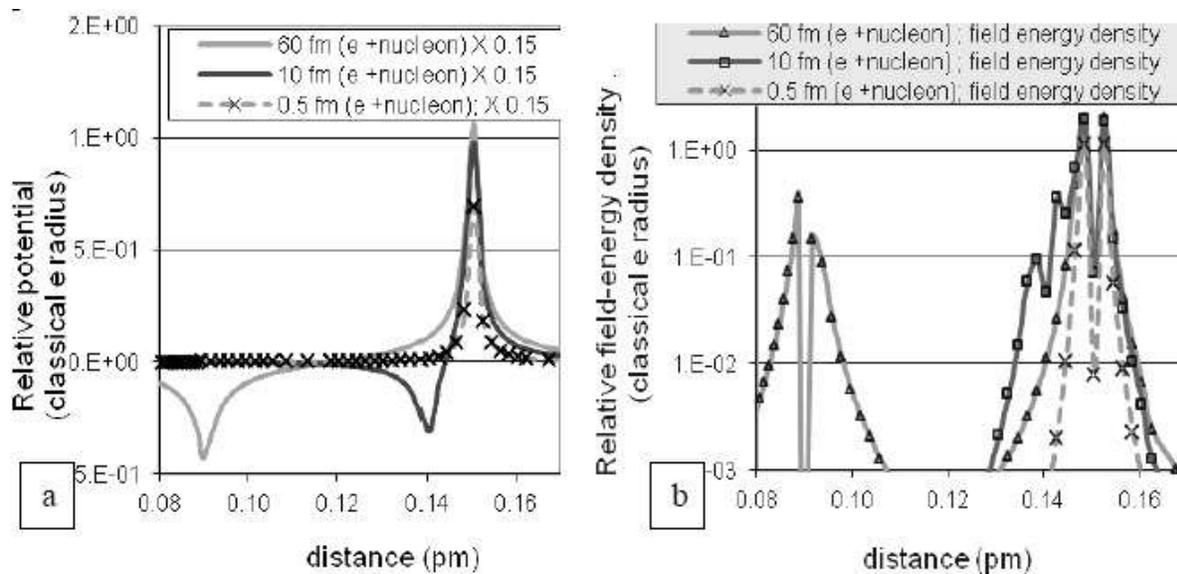


Figure 2. (a) Electric potential between, and (b) EM mass-energy distribution of, an electron (assuming a classical radius) and proton separated by 60, 10, and 0.5 fm. Note change in “size” of both particles as they approach each other and the change in vertical scale between (a) and (b).

We have shown how the Coulomb-barrier problem might be solved with the lochon model and laid a foundation for the D–D nuclear interaction with the help of tightly bound, highly energetic electron pairs (lochons). Now we further extend the model to see how it affects the nuclear interaction.

3.3. Nuclear interactions

Examining the traditional D–D to $^4\text{He}^*$ transition (Fig. 3, where * indicates an excited state of the nucleus), we see the broad transition region (bracketed) beyond 23.8 MeV above the ^4He ground state. This “ Q ” value (broad arrow at 23.8) is the energy difference that corresponds to the mass difference between the deuterium pair and the ^4He atom. Even with the improbable event of D–D tunneling from zero kinetic-energy states, the excess mass of the deuterium atoms would put the deuterons into this high level. These excited $^4\text{He}^*$ states are above the fragmentation levels at ~ 20.6 and 19.8 MeV (dashed arrows). While fragments from both levels have been observed in LENR experiments, the radiation fluence levels are not nearly high enough to explain the excess heat observed. Furthermore, the measured concentration levels of ^4He have been orders of magnitude higher than would be expected from standard theory and, in some cases, have been high enough to account for the observed heat if all excited-state energy (~ 24 MeV) is converted to thermal energy [21]. How could this happen? Since the observed data is not possible within the known framework of nuclear physics, something else must be going on.

This figure, which shows the excited states of ^4He as well as the fragmentation and minimum D–D input energy levels, indicates that there are no energy levels below the $^3\text{H} + \text{p}$ fragmentation level. Thus, even if a helium nucleus were to be excited into a heretofore-unobserved meta-stable state below the 20.2 MeV level, it might still fragment rather than decay back to the ^4He ground state. Likewise, in a d–d interaction, if fusion via normal tunneling were to take place, it would be resonance tunneling into one of the many levels above the broad arrow at 23.8 MeV. Decay from these excited states would almost always give nearly equal probabilities of fragmentation into the p or n fragmentation channels.

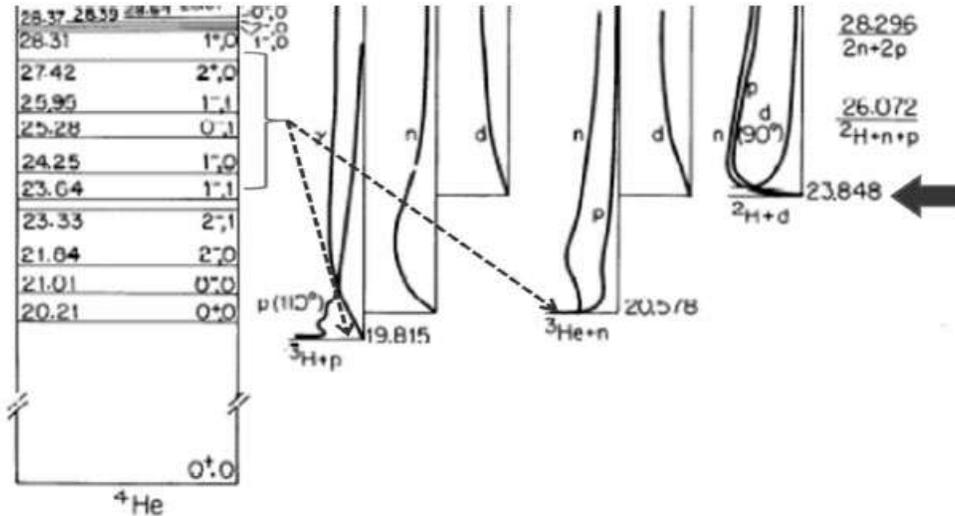


Figure 3. Energy levels and possible decay branches associated with conventional D–D to $^4\text{He}^*$ fusion reactions, as well as the excited states and fragmentation and minimum d–D input energy levels of ^4He [10]. Note that these values include the mass energy of the atomic electron(s).

However, if the excited state is able to more quickly decay to one of the levels below 23.8 MeV, the fragmentation probability begins to shift to favor the proton channel. This enhanced decay into the lower excited states could be an explanation for reduced levels of neutrons for the heat generated. However, it does not explain reduced levels of energetic protons.

3.4. Reduced energy $^4\text{He}^*$

With the ability of deuterons to be drawn from an appropriate PdD lattice site through the lattice and nuclear-Coulomb barriers to an adjacent reduced-energy nucleus (Appendix A) of a D^- ion, the possibility of a low-energy excited compound nucleus becomes real. With the lochon (the shrunken-orbit electron pair – as indicated by the superscript #) rather than with the normal atomic electrons, the excited (but lochon-neutralized) helium-4 nucleus may not have sufficient energy to fragment. Since gamma decay is highly forbidden, how does $^4\text{He}^{*\#}$ shed the excess energy to get to the ^4He ground state? It is proposed that existence of this condition and the subsequent decay process is the basis for the experimental observations of CMNS.

Depending on the actual energy of the excited (compound) nuclei, the decay process could include fragmentation, or not. Since there may be no standard resonance states of this compound nucleus, the final tunneling could be into a range of energy levels. This variability would account for the observations in CMNS of excess heat, in both p–p and d–d reactions, and the observations (or absence) of tritium, ^3He , neutrons, and ^4He in the d–d reaction. The unpredictability of experimental results has been a major problem for CMNS. It now may be a validation of the extended-lochon model. Furthermore, this proposed mechanism accounts for observed “transmutation,” something that many CMNS investigators did not accept for a long time.

To see how this “new” process can occur, we must take a closer look at the details behind Fig. 3. If an appropriate state existed below ~ 19 MeV, then any fragmentation would become unlikely. We propose a non-fragmentation mechanism that does not rely on a new state below 20 MeV. This mechanism of tightly bound electron(s) could shift the

existing ^4He ground and excited nuclear states down and it demonstrates how the fragmentation levels can be shifted up in energy.

The key to the mechanism is the lochon, which during the collision process attains significant energy (keV to MeV range); but, being tightly bound in an $l = 0$ ground state, it does not radiate. If it survives the final tunneling of the d^+ through the thin residual $D^{-\#}$ (actually d^+ plus lochon) Coulomb barrier, it may have attained MeV energies from the work done at the expense of the D^- Coulomb potential energy. Thus, it is very tightly bound and the lochon, the D^- nucleus, and the deuteron all have had mass converted into kinetic and field energy. Since the average lochon orbital radius is so small, even in a circular orbit, the orbital angular momentum is much less than \hbar . (so that the $l = 1$ state is not available). With the lochon being spin-coupled electrons in a filled s-orbital, there is no spin-flip possible to provide angular momentum sufficient to generate a photon. Therefore, no photonic radiation is possible and there is no violation of the uncertainty principle as the lochon orbit and size both shrink during the D^-D^+ collision.

Once the D^+ is inside the D^- Coulomb barrier, the situation is different from that of the normal d–d scattering problem. The normal situation compares the mass difference between ^4He and $2D$, which is just the same as that between $^4\text{He}^{++}$ and $2d$. In our case, the electrons and protons in the helium nucleus with a tightly bound electron pair and the free deuterium atoms are different animals. ($^4\text{He}^*$ is the excited state with normal atomic electrons, and $^4\text{He}^{*\#}$ is $^4\text{He}^*$ with shrunken-orbit electrons.) The external Coulomb field of these “shrunken-orbit” electrons (a source of their mass) is nearly zero, and a comparable amount has been subtracted from the proton(s) fields. This mass–energy equivalent has been converted into kinetic energy [22] and into the interactive-field energies (mutual attractions and repulsion of the electrons and protons).

The nuclear potential is much different also. The Coulomb barrier between the lochon-altered protons (now electric dipoles) is almost gone. Thus, they can be much closer together. (In the d–d case, all 4 nucleons can then be closer together.) Since most of the normal nucleon wavefunction is outside the d–d nuclear well, the depth of the $^4\text{He}^{*\#}$ nuclear potential well with which the nucleons are bound is increased by the loss of Coulomb repulsion and the gain in time spent in the well (increased wavefunction overlap). As a consequence, the “effective” depth of the nuclear well is further increased, the ground and excited-state energies become lower, and the energy required to break apart the excited nucleus is higher. If we look at Fig. 4 (with this information applied to Fig. 3), we see that the whole column on the left is moved down (the energy levels may split and, depending on the model used to describe the new nucleon - dipole or light proton, their values will be different) and everything on the right (except for the arrow) is moved up.

The Q arrow at 23.8 MeV moves down with the column; because, while the energy distribution of the $^4\text{He}^\#$ and $^4\text{He}^{*\#}$ (which states may never actually exist) is different from that of ^4He and $^4\text{He}^*$, the mass difference between $^4\text{He}^\#$ and $2D^\#$, is still nearly the same (the protons have lost about the same mass that the lochon has gained). Thus, the deuterons tunnel into nearly the same states that they would have without the energy reduction. However, with the tightly bound lochon, the states are no longer the same states. And, if they were stable states, they would be shifted down in energy (along with the ground state if it exists with the lochon).

4. Fragmentation

Do the $^4\text{He}^{*\#}$ fragmentation levels really rise above the 23.8 MeV D–D energy level? Well, the elimination of nucleon Coulomb repulsion is considered to decrease the ground-state level by about 0.73 MeV (but that is based on comparisons of isomers differing by only one atomic number). If we consider a lochon in the nuclear region, the difference resulting from the double-negative charge could be 1–2 MeV (the increase in nuclear binding energy, which also raises the relative fragmentation energies by at least that amount). Since fragmentation energy is a strong function of inter-nucleon distance, and the lochon has such a great impact on that, this energy could easily go up by another MeV or two. So the answer is seen in Fig. 4. The lowest “ $^4\text{He}^{*\#++}$ + lochon” fragmentation level is above not only ~ 22.8 MeV, it may be above the $Q^\# = 23.8$ MeV value. The number of fragmentation levels of the lochon-neutralized nucleus may

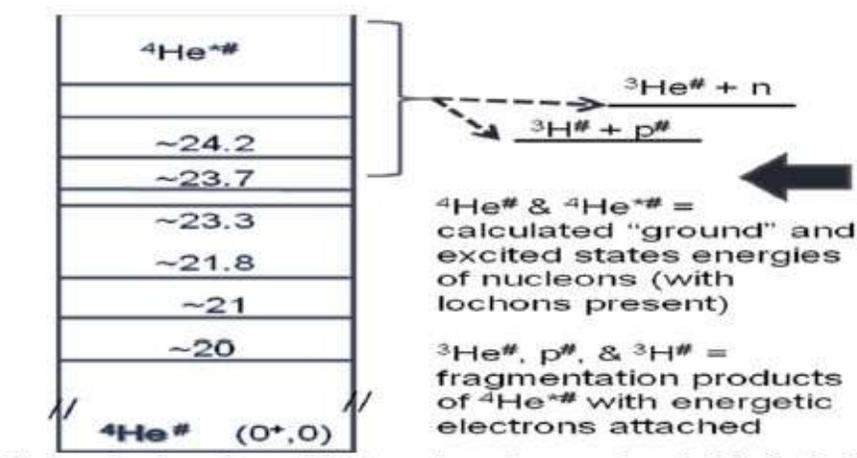


Figure 4. Energy levels and possible decay branches associated with the lochon model D + D to ${}^4\text{He}^{*\#}$ fusion reactions and minimum D + D input energy levels of ${}^4\text{He}^\#$. Note that these values include the tightly bound-electron-induced adjustments to the nuclear potential and the mass energy of the atomic and shrunken-orbit electrons.

be increased because the neutrons and tightly bound electrons can be divided in multiple ways among the two protons involved. These levels can be considered as representative of centrifugal barriers since it takes increased kinetic energy and angular momentum to get to them.

This lochon modification of the compound nucleus (${}^4\text{He}^{*\#}$) energy levels can thus explain the absence (or change in ratio) of fragmentation in LENR identified as item 2 in the introduction.

5. Alternative Decay Paths

Perhaps important for the reduction of fragmentation is the number of accessible shrunken-orbit nuclear-energy levels proposed to be now below the fragmentation levels. Any occupied levels above the ${}^3\text{He}^\#$, $p^\#$, and ${}^3\text{H}^\#$ fragmentation levels are transitory (rapidly fragmenting or decaying to these lower-energy levels). In addition to their normal decay processes (which do not compete well with fragmentation), the excited nucleons may reach lower-energy stable levels by transferring their kinetic energy to their tightly bound electrons. These electrons couple this energy to the nearby atomic electrons or the lattice (via near-field radiation, phonon, and plasmon interactions). In the presence of this new decay process, normal decay processes from excited-nuclear levels ${}^4\text{He}^{*\#}$ to the fragmentation or lower levels is inhibited and becomes a low-probability process.

An important point to note is that the new energy-transfer process to and through the tightly bound electrons is not rapid. It is steady. But, even for states above fragmentation levels, this initial decay process may compete well against fragmentation. Furthermore, the presence of the tightly bound electron(s) interferes with “normal” decay processes that depend on stable resonance states (e.g., gamma decay) and/or angular momentum (e.g., fragmentation). The steady process means that the total time for decay to ground is long, relative to normal decay modes. However, it “drains” EM field energy necessary for the formation of gamma rays and utilizes the angular momentum that would allow fragmentation. While it is slowing these processes, it lowers the nuclear energy below the fragmentation levels and interferes with the stability of the lower nuclear states shown in Fig. 4. Thus, as long as the tightly bound electrons are present, the helium nucleus is not in a normal state and the indicated excited levels are only representative and cannot be considered real.

The presence of a lochon so-greatly reduces the Coulomb barrier to fusion, that non-zero-angular-momentum ${}^4\text{He}^{*\#}$ states might become accessible. These states are more accessible via shrunken-orbit electrons and their decay through normal processes (e.g., gamma decay to lower levels, or to the ground state) could more readily compete with fragmentation. Nevertheless, it is unlikely that gamma decay from such states (or direct tunneling to the stable-fragments) could compete with the energy decay process from proximity coupling through, or in the presence of, the tightly bound electron(s) or lochon.

During the p–p or d–d lochon-enhanced fusion process, the lochon could divide or perhaps attain energies in the MeV range from coupling with the protons accelerating in the nuclear potential. These rapidly accelerating and decelerating electrons would then radiate Bremsstrahlung or would proximity couple their energy to the adjacent Pd electrons [23]. This extended-collision/radiation process lasts:

1. Until the neutral entity (${}^2\text{He}^{*\#}$ or ${}^4\text{He}^{*\#}$) drifts into a neighboring nucleus in a transmutation process;
2. Until one (or more) of the shrunken-orbit electrons combines with a proton ($p + e \Rightarrow n + \nu$, via the p–e–p, p–2e–p, etc. reactions); or,
3. Until ejection of the energetic electron(s) from the nucleus and the (D or ${}^4\text{He}$) ground state is reached.

Thus, the last of the introductory arguments against cold-fusion have been addressed.

6. Conclusion

The Lochon Model provides a basis for penetration of the nuclear Coulomb barrier in low-energy p–p and d–d fusion reactions. Depending on the actual energy of the excited (compound) nuclei and the number of tightly bound electrons, $e^\#$, still attached (0, 1, or 2) after the nuclear Coulomb barrier has been penetrated, the decay process could include fragmentation, or not. This extension of the model accounts for the observations in CMNS of excess heat, in both p–p and d–d reactions. It also explains the observations (or their absence) of tritium, ${}^3\text{He}$, neutrons, and ${}^4\text{He}$ in the d–d reaction. The ability of the tightly bound lochon - to alter energy levels in the nuclear potential wells and fragmentation energies of the excited ${}^2\text{H}^{*\#}$ and ${}^4\text{He}^{*\#}$ atoms - permits decay to the ${}^2\text{H}$ or the ${}^4\text{He}$ ground states or allows sufficient time as a shrunken-orbit atom or neutral nucleus for transmutation of lattice atoms or impurities.

Variation of observed results of LENR is thus based on the number of tightly bound, energetic electrons remaining within the nuclear region after initial D^-D^+ fusion and during the subsequent decay process. The Extended Lochon Model, in its present form, may explain all observed LENR processes (model-predicted levels and observability of Bremsstrahlung and any neutrinos must still be determined), but not necessarily the best means of, or materials for, producing them. That comes next.

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Appendix A: Development of Electron Coupling into Tight Orbits

For the reasons stated above and in our earlier work, the D^-D^+ pairs are formed within the loaded PdD lattice (or interface and defect regions). This phonon-induced charge polarization is a maximum during the closest encounter of the deuteron ions. At this point, the monopole–monopole interaction is highest and the resulting E field can exceed the phonon field, to strip one or both electrons from the D^- ion. This exchange thus forms molecular deuterium (perhaps only temporarily, if the lattice barrier separates the molecule rather than drawing it into one lattice site).

This appendix addresses the electron energies and their exchanges assuming that the electrons are maintained as a pair long enough to move too deep into the D^- potential well to be removed by the D^+ E field until after Coulomb barrier penetration. The problem is addressed as a monopole–monopole interaction with the deepening electron energy levels treated as a modified Stark Effect. (The electron-energy levels in the D^- ion deepen in the E fields produced by the lattice and then by the D^+ ion.)

Of importance to the lochon model is the fact that the electrons in the D^- do work and, thereby, move deeper into the Coulomb potential well. Therefore, we need to compare the change in potential between the D^- and D^+ ions (ΔV_{dd}) relative to the work done in bringing them closer together (from l_1 to l_2) by a small distance, $\Delta l = l_1 - l_2$. In the simplest model, for the conditions of a $D^- D^+$ Coulomb attraction much greater than phonon effects and for a dielectric constant of ϵ ,

1. Change in potential: $\Delta V_{dd} = -e^2(1/l_1 - 1/l_2)/\epsilon \approx (e^2/\epsilon(l_1 l_2))\Delta l$. (Thus, for small Δl , $l_1 \approx l_2 \approx l \Rightarrow \Delta V_{dd} \approx (e^2/\epsilon l^2)\Delta l$.)
2. The force between the ions: $F_{dd} = -dV_{dd}/dl = -e^2/\epsilon l^2$.
3. Work by each deuteron ion: $\Delta W_1 = \Delta W_2 = F_{dd} * \Delta l/2 \approx (-e^2/\epsilon l^2)(\Delta l/2)$.

The $\Delta l/2$ term comes from the near-equal masses of the D^- and D^+ . The work done by the D^- electrons equals that done by the D^+ ion. Each ion moves the other by $\frac{1}{2}$ the change in total separation distance Δl . The total work of the $D^- D^+$ system ($\Delta E_{dd} = \Delta W_1 + \Delta W_2$) is approximately the potential difference between l_1 and l_2 . We can look further into the conservation of energy to see where the work comes from. The D^+ ion does work by converting some of its field energy into kinetic energy (and in overcoming the lattice barrier early in the process). The D^- ion does the same; but, what field energy is converted? It must be the negative portion.

The lochon provides the negative charge and therefore the D^- ion portion of the work and field energy to bring the deuterons together and to give them kinetic energy to overcome the lattice barrier. In providing this energy, the lochon drops deeper into the D^- potential well and gains kinetic energy. These distances of the changing lochon orbits (charge = $-2e$, mass = 2 electron masses) relative to the D^- nucleus equal r_1 and r_2 with $r_1 > r_2$. Things are different from above because we are now looking at many electron orbits rather than only a portion of a single phonon cycle. The D^- nucleus does not significantly change its KE relative to the lochon during a decay of the lochon orbit. Therefore the lochon does almost no work on its deuteron nucleus in the D^- center-of-mass system. (It does not move the deuteron within this system; but, it moves the whole D^- relative to the D^+ .) However, the nucleus does work on the lochon. The lochon gains $\Delta V_{dl}/2$ in KE from the orbit decay and (from the virial theorem) can do the same amount of work on the $D^- D^+$ ion pair. Again, assuming that the $D^- D^+$ interaction energy greatly exceeds that of the lattice barrier:

4. Δ in potential (D^- nucleus & lochon): $\Delta V_{dl} = -2e^2(1/r_1 - 1/r_2)/\epsilon = 2e^2/(r_1 r_2) * \Delta r$.
5. Work done in decay of D^- electrons: $\Delta W_{dl} = \Delta V_{dl}/2 \approx (e^2/\epsilon r^2)\Delta r$.

Assuming that the model holds, and if $\Delta V_{dl}/2 = \Delta W_1 = \Delta V_{dd}/2$ (e.g., if $\Delta r/r^2 = \Delta l/2l^2$) and $l > 2r$, then $\Delta l > 8\Delta r$. Thus, unless early in the process the lochon has moved deeply into its potential well, the inter-deuteron distance rapidly shrinks to the lochon orbit radius [24] ($l = r$) and will share the bound electrons. Sharing the electrons (lochon) between the deuterons will increase the size of the electron distribution and eliminate the $D^- D^+$ Coulomb attraction. If the electron orbit has shrunk prior to the transition from $D^- D^+$ to $D-D$, the now tightly bound electrons still provide better screening than that from free electrons or from normal molecular electrons. Furthermore, the momentum of the deuterons will continue to close the deuteron gap and thereby further shrink the electrons' (now molecular) orbit. The later the sharing of electrons, the deeper the electrons will be in their potential well, the higher the deuteron momenta, and the smaller the Coulomb barrier that must be tunneled through. Therefore, the phonon-induced collision process at the lattice barrier is the starting point that can lead to, or block, the proposed extended-lochon model.

The deuterium sites in PdD are highly confined by the Pd lattice and screened from each other by the Pd-lattice electrons. Thus, the initial conditions are not amenable to any simple analysis. Since, work done by the bound-electron pair in overcoming the lattice barrier may be critical to the model; it must be addressed in a more sophisticated manner than is possible in this paper.

As described here, the lochon motion to deeper regions of the D^- potential well (i.e., to tighter orbits with increased kinetic energy) can proceed without any radiation. Nevertheless, mass energy of both deuterons is lost (Appendix B). The process of shifting between the normal D^- ion in a lattice site to a “reduced-energy-nucleus” ion at the lattice barrier is reversible (unless, or until, the deuteron nuclear potentials overlap) and can continue to oscillate at the phonon frequency. However, with sufficient deuteron and boson energies within the Coulomb wells, energetic-lochon-catalyzed fusion may occur as described in the text. Alternatively, the “shrunk” electron orbits at the point near deuteron collision may allow closer approach of the D^-D^+ pair and the resultant stronger coupling would permit the small D^+ ion to be drawn into the D^- ion’s lattice site. The now-allowed proximity of the deuterons, one perhaps with electrons in the metastable nought orbit (Appendix C), can thereby provide boson-catalyzed fusion (similar to muon-catalysed fusion).

Appendix B: Electron Size in the Nuclear Regions

This appendix addresses the “size” of an electron as it must be pictured in its interaction with protons at nuclear distances. It is based on the presently-accepted model that the mass of the electron is totally electromagnetic [25]. Furthermore, the electrostatic field defining the charge is assumed to be the dominant EM component. The proton’s external EM field is identical to that of the electron. Therefore, if size is based on charge field alone, the electron and proton would be the same size. However, since the Compton radius is based on total mass and proton mass from the charge field is only a very small percentage of the proton mass energy, this useful radius is much smaller for the proton than is that for the electron. On the other hand, when the electron and proton are close together, other things come into play. Of major importance is the “collapse” of electron size as its far-field component is cancelled by that of the proton and the long-range monopole potential becomes only the short-range potential of a dipole (Fig. 2a). Other things happen as the electron and proton approach one another.

The additional kinetic energy of tightly bound electrons $e^\#$ means that an electron “size,” based on the deBroglie radius ($\lambda_{dB}/2\pi$), shrinks as $\lambda_{dB} = h/mv$. While this is actually related to the time-averaged electron-charge distribution in an orbit, not any actual electron size itself, there is still a frequency associated with the orbit and thus the deBroglie wavelength. Since frequency is related to energy and energies are additive, the deBroglie frequency (related to the deBroglie wavelength, $\nu_{dB} = v/\lambda_{dB}$) is added to the Compton frequency (related to the Compton wavelength, $\nu_C = c/\lambda_C$) and the summation provides a higher frequency (hence energy: $E_t = h(\nu_1 + \nu_2)$) that gives a smaller electron radius. (This shrinking is a basis for association with the momentum/size relationship of the Heisenberg Uncertainty Principle.)

A poor understanding of the various relationships between electron size and time-averaged charge distribution is a common source of some miscalculations of Coulomb screening by electrons. For example, tunneling is considered to be instantaneous. Therefore, screening by an electron “cloud” is not an average value, but a statistical probability of finding an electron at a given location at the instant of tunneling. This appendix provides some further insight into different usages of electron sizes.

If the much larger Compton electron radius is assumed, rather than the classical radius, one might think that the change in electron shape and effective charge begins much further from the proton. However, in Fig. 2a, because the plotted potential is a $1/r$ function (and the total energy and charge is fixed), the actual amplitude and shape of the exterior electron field cannot change with the model. The difference must be in the definition, not in the particle. With a Compton radius of 384 fm (0.384 pm), the statement would then be that the electron’s “size” extends much further to the extremities of the field than does the classical-electron radius of 2.82 fm. If the potential “inside” the chosen electron

radius is different, then the field in that region will change and the magnitude of the total field must be renormalized to provide the total mass/field energy of the electron.

Assuming that the electron mass is entirely electromagnetic in origin and that the field-energy density is proportional to the field squared, then the mass-distribution of the electron can be pictured as much more localized than that of the potential distribution (Fig. 2b). (Field \mathbf{E} is proportional to the derivative of the potential, giving $1/r^2$ dependence. This implies that energy density E , proportional to \mathbf{E} squared, varies as $1/r^4$.) The external-EM portion of the proton energy can be pictured in a similar manner. (Remember that this charge-field component is only about 0.05% of the total proton mass.) Because of the great increase in localized mass density relative to the potential, Fig. 2b is shown as a semi-log plot of the non-relativistic charge-field energy only. If the proton's mass energy (held to be relativistic-field energy by one author - AM) were included in the figure, it would extend 3 orders of magnitude above the curves shown. Expanding the resolution of the electron EM mass profile (not shown), one could see that the classical radius includes >99% of the mass energy. The Compton radius of the electron extends to some very-low value of field or potential. The electric potential at the 0.15 fm Compton radius of the proton is still very high (Fig. 2a).

Assuming that charge particles are not singularities, the electric potential must be finite and must reverse at the center of the charges. Therefore the field-energy density goes to zero at this point. However, as the electron approaches the proton at 10 fm distance in Fig. 2b, this electric-field density (mass) of the electron disappears. The electron may no longer have an identity. Nevertheless, when the electron gets close enough to the proton to eliminate any sign of the electron's negative charge, there is still a residual positive charge of the proton. The difference in near-field "charge" between the electron and proton is a relativistic effect. This is a result of the need to have the $1/r$ potential continue to a smaller radius for the proton than for the electron. It takes energy to do this.

The figures described above are for localized charges. They indicate that, when the electron is within Fermis of the proton, its field-energy density disappears. Where does it come from and where does it go? It comes from the proton and electron electrostatic fields and goes into motion of the altered and residual field energy (mass and/or charge). Unless energy is radiated away, or is transferred in some other form, it is bound to the "compound structure" and acts as energy-equivalent mass. However, the moments of inertia, magnetic moments, etc. of the structures are altered and energy can be stored in the new angular motion. For an isolated electron-proton structure, this has little consequence (also it is an extremely short-lived condition - a single transit by the electron?) However, for colliding p^+p^- or D^+D^- structures (where the closely bound electrons may exist for hundreds of orbits or more), it means that the nucleon wave-functions are altered.

Appendix C: Nought-orbits ($n = 0$)

In 2005, Jan Naudts posted a paper [19] on the arXiv entitled "On the Hydrino State of the Relativistic Hydrogen Atom." He showed that there was a solution to the Klein-Gordon (K-G) equation that is generally rejected as being non-physical. This solution adds a new atomic orbital at close to mc^2 . Since the K-G equation pertains to Bosons, not Fermions, Naudts suggested that the question of square integrability of the Dirac equation (which blocks Fermions from that level) might be the non-physical requirement instead and thus the K-G solution could be used to support such a level for Fermions as well. Two papers [26,27] have rejected both suggestions; but, a third [28] has accepted the K-G solution as real.

Applying this information to our model and assuming the additional K-G solution to be valid (at least for bosons), the reality of the bound electron pair (the lochon) as a boson means that this level is available as a physically real lower-energy state (the $n = 0$ or nought-orbital). This level will not be explored further here (such as the effects of a doubly charged boson on the solution). However, neither the $n = 1$ ground state nor the $n = 0$ nought orbit has sufficient angular momentum to permit photonic-energy transfer. Therefore, it is still a forbidden photonic transition. Nevertheless, as a viable, tightly bound, relativistic-electron state, the nought level can be reached by the model described in this paper

and it provides additional basis for the extended-lochon theory of low-energy nuclear reactions. This could be a critical point for both the Coulomb barrier penetration and the energy level at which the H–H or D–D fusion begins.

A potential importance of this nought orbit is the fact that it provides an intermediate stage for fusion via a mode that is well-known physics - muon-catalysed fusion. Since the $n = 0$ electron-orbit radius is ~ 400 fm (at ~ 507 keV), $n = 0$ hydrogen would be smaller than muonic hydrogen. But, just as a filled orbital H^- ion is larger than the neutral atom, the lochonic $n = 0$ hydrogen ion would be larger than a neutral nought-orbit atom. On the other hand, the nought-orbit molecule ($H^+ + H^-$, or $H_2^\#$) might be smaller than the muonic hydrogen molecular ion (and perhaps ionically bound rather than covalently bound). Details must be presented elsewhere; but, the implications for nought-orbit hydrogen and molecules for lattice mobility, lattice-site double occupancy, and muon-catalysed-type fusion are immense. Whether this is an unreal, a competitive, an incidental, or an assisting process is still to be determined.

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